

7. The ratio of the weight of Benjamin to that of Jack is 5 : 3, while the ratio of the weight of Benjamin to that of Peter is 4 : 7.

(a) Find the ratio of the weights of Benjamin, Jack and Peter. (6 marks)

Ratio of B : J : P
= 20 : 12 : 35

$$\begin{array}{r} B : J : P \\ 5 : 3 : 7 \\ 4 : 7 : 35 \\ \hline 20 : 12 : 35 \end{array}$$

(b) If the weight of Jack is 30 kg, find the weights of Benjamin and Peter. (12 marks)

Or, Weight of B = $\frac{5}{3} \times 30 = 50$ kg
Weight of Peter = $\frac{7}{3} \times 30 = 70$ kg

8. The capacity of a swimming pool is 1 080 m³.

(a) The pool has been empty originally and is now filled up with water at a speed of 3.6 m³/min by a pipe. How much water is filled in two hours? (6 marks)

2 hours have $2 \times 60 = 120$ min

$(3.6 \times 120) \text{ m}^3$ of water can be filled in 2 hours
= 432 m³

(b) Suppose after filling the pool for two hours, the speed of water filling the pool increases to 4 m³/min. How long does it take to fill the swimming pool completely? (8 marks)

Volume of water need to be filled:
 $(1080 - 432) \text{ m}^3$
= 648 m³

extra Time = $\frac{\text{distance}}{\text{speed}} = \frac{648 \text{ m}^3}{4 \text{ m}^3/\text{min}}$

= 162 min

= 2 h 42 min

\therefore To fill the pool completely need 2 h 42 min + 2 h
= 4 h 42 min
or 4.7 hr.

— End of Paper —

Name : _____ ()

Class : _____ Date : _____

Marks : _____ /100

CHAPTER 12

Ratio and Rate

[Time allowed: 35 minutes]

1. Express the rates of the following in the units stated in the brackets.

(a) A lion eats 91 kg of meat per week. (kg/ day) (4 marks)

91 kg / week
= 91 kg / 7 days
= 13 kg / day

(b) 161 candies weigh 0.7 kg. (candies/ kg) (4 marks)

161 candies / 0.7 kg
= $161 \div 0.7$ candies / kg
= 230 candies / kg

$\begin{array}{r} 230 \\ 7 \overline{) 1610} \\ \underline{14} \\ 21 \end{array}$

(c) The selling price of 0.3 kg of cheese is \$17.4. (\$/ kg) (4 marks)

\$17.4 / 0.3 kg
= $174 \div 3$ / kg
= \$58 / kg

2. It is given that the length of 2 mm on a map represents the actual length of 0.5 km. Find the scale of the map in the form of 1 : n. (8 marks)

Scale = $\frac{\text{map}}{\text{real}}$
= $\frac{2 \text{ mm}}{0.5 \text{ km}}$
= $\frac{2 \text{ mm}}{0.5 \times 1000 \times 100 \times 10}$
= $\frac{2 \text{ mm}}{500000 \text{ mm}}$
= 1 : 250000

3. The selling price of 500 g of steak is \$550.

(a) Find the selling price of steak in \$/g. (6 marks)

$$\begin{aligned} & \$550 / 500 \text{ g} \\ & = \$550 \div 500 / \text{g} \\ & = \$1.1 / \text{g} \end{aligned}$$

The selling price of steak is \$1.1/g

(b) How much steak in kg can be bought for \$1 650? (6 marks)

$$\begin{aligned} & (\$1650 \div \$1.1) \text{ g} \div 1000 \text{ g} \\ & = (1500 \div 1000) \text{ kg} \\ & = 1.5 \text{ kg} \end{aligned}$$

$$\begin{array}{r} 1500 \\ 11 \overline{) 16500} \\ \underline{11} \\ 5500 \\ \underline{55} \\ 0 \end{array}$$

\therefore \$1650 can buy 1.5 kg of steak.

4. On a floor plan with the scale of 1 : 300, the length and width of a bedroom are 8 cm and 7 cm respectively.

(a) Find the actual dimensions of the bedroom. (Give your answer in Length \times Width.) (6 marks)

$$\begin{aligned} & \text{The actual dimensions:} \\ & 8 \text{ cm} \times 300 \text{ by } 7 \text{ cm} \times 300 \\ & = 2400 \text{ cm by } 2100 \text{ cm} \\ & = 24 \text{ m} \times 21 \text{ m} \end{aligned}$$

(b) Find the actual area of the bedroom in m^2 . (6 marks)

$$\begin{aligned} & \text{The actual area:} \\ & 24 \text{ m} \times 21 \text{ m} \\ & = 504 \text{ m}^2 \end{aligned}$$

$$\begin{array}{r} 24 \\ 21 \\ \hline 48 \\ 24 \\ \hline 504 \end{array}$$

5. Suppose we can exchange 4 Japanese Yen for 0.3 Hong Kong dollar and 2 Euro for 25 Hong Kong dollars.

(a) How much Hong Kong dollars can we exchange for 100 000 Japanese Yen? (6 marks)

$$\begin{aligned} \frac{4}{0.3} &= \frac{100000}{x} \\ x &= 100000 \times \frac{0.3}{4} \\ &= 7500 \end{aligned}$$

Jep	Hk\$
4	0.3
100000	x

\therefore 7500 HK dollars can be exchanged for 100 000 Japanese Yen

Japanese	Hong Kong	Euro
4	0.3	2
100	7.5	0.6
x	10000	
100000	7500	600

We can exchange 7500 HK dollars

(b) Hence, how much Euro can we exchange for 100 000 Japanese Yen? (6 marks)

$$\begin{aligned} \frac{7500}{25} &= \frac{x}{2} \\ x &= \frac{7500}{25} \times 2 \\ &= 300 \times 2 \\ &= 600 \end{aligned}$$

HK	Euro
7500	x
25	2

\therefore 600 Euro can be exchanged for 100 000 Japanese Yen

From the above table
100000 HK dollars can exchange for 600 Euro

6. A car travelled 105 km in 1.4 hours.

(a) Find the speed of the car in km/h. (6 marks)

$$\begin{aligned} & 105 \text{ km} \div 1.4 \text{ hours} \\ & = \frac{105}{1.4} \text{ km/h} \\ & = 75 \text{ km/h} \end{aligned}$$

$$\begin{array}{r} 75 \\ 14 \overline{) 1050} \\ \underline{98} \\ 70 \\ \underline{70} \\ 0 \end{array}$$

The speed of the car is 75 km/h

(b) If the speed of the car increases by 5 km/h, find its travelling distance in 45 minutes. (6 marks)

$$\text{New speed} = (75 + 5) \text{ km/h} = 80 \text{ km/h}$$

$$\begin{aligned} \text{Distance travel} &= \text{speed} \times \text{time} \\ &= 80 \text{ km/h} \times 45 \text{ min} \\ &= 80 \text{ km/h} \times \frac{45}{60} \text{ h} \\ &= 80 \text{ km/h} \times \frac{3}{4} \text{ h} \\ &= 60 \text{ km} \end{aligned}$$

\therefore The travel distance is 60 km in 45 minutes